
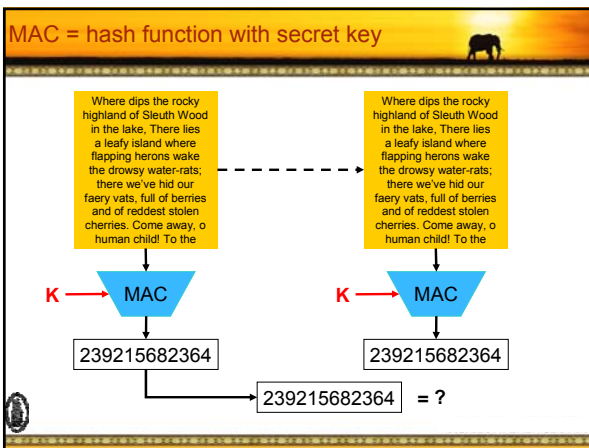
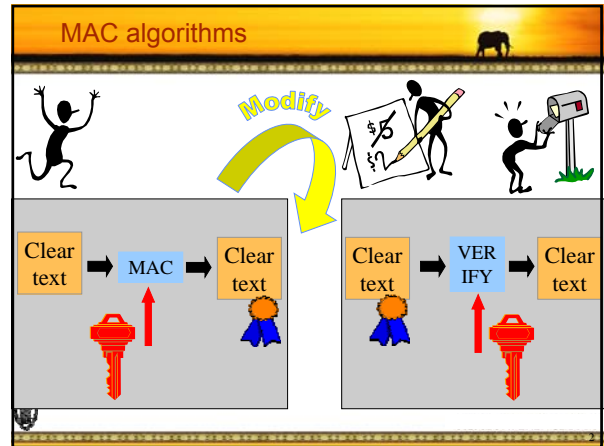


## MAC Algorithm Design and Cryptanalysis: Basics

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### MAC: Definition

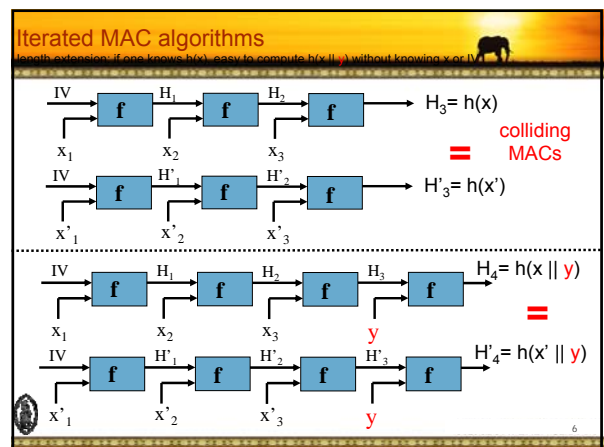
**Message Authentication Code**  
= hash function with secret key:

1. Description of  $h$  public
2.  $X$  arbitrary length  $\Rightarrow$  fixed length  $m$  (32... 160 bits)
3. Computation of  $h_K(X)$  "easy" given  $X$  and  $K$
4. Computation of  $h_K(X)$  "hard" given only  $X$ , even if a large number of pairs  $\{X_i, h_K(X_i)\}$  is known

- Calculation of  $h_K(X)$  without knowledge of secret key: *forgery* (verifiable or not verifiable)

### MAC: generic attacks

- 1. Guess MAC:**  $\pm$  same as for hash function
  - On-line verification only
  - Not verifiable
  - Success probability max (1/2<sup>m</sup>, 1/2<sup>k</sup>)
- 2. Exhaustive key search:**  $\pm$  same as for block cipher
  - #  $X, h_K(X)$  pairs =  $k/m$
  - # attempts =  $2^{k-1}$
- 3. Birthday paradox on iterated MAC algorithms**  
Internal memory  $n$  bits; result  $m$  bits (output transformation  $g$ )  
Forgery after  $2^{n/2}$  known and  $\leq 2^{n-m}$  chosen texts



### Collision attack on iterated MAC algorithms

- Collision in MAC values leads to trivial forgery after 1 chosen text-MAC pair
  - indeed:  $h(x) = h(x') \Rightarrow h(x \parallel y) = h(x' \parallel y)$
- If an opponent queries  $h(x \parallel y)$ , he can forge  $h(x' \parallel y)$
- MAC value of  $m$  bits: need  $2^{m/2}$  known text-MAC pairs to find a MAC collision

### Iterated MAC algorithms with output transformation

- If  $g$  is a injective (fewer input bit than output bits):
  - $h(x) = H_4 = H'_4 = h(x')$  but it may be that  $H_3 \neq H'_3$
- If  $H_3 \neq H'_3$  the attack will likely fail:  $h(x \parallel y) \neq h(x' \parallel y)$
- Conclusion: attack requires that  $H_3 = H'_3$  (**internal collision**)

### Collision attack on iterated MAC algorithms

- Solution: simulate the first attack
- For all MAC collisions ( $h(x) = h(x')$ ) also ask for  $h(x \parallel y)$  and  $h(x' \parallel y)$
- If  $h(x \parallel y) = h(x' \parallel y)$ , we have likely found an internal collision (a collision for  $H_3$  in our example)
- Attack complexity:  $2^{n/2}$  known text-MAC pairs and  $2^{m-n}$  chosen text-MAC pairs

### MAC based on a block cipher: CBC-MAC

- Standards (ANSI, ISO, IEC)
- Proof of security by [Bellare-Kilian-Rogaway]
- $m = 32 \dots 64$  bits
- Special operation for last block is essential: EMAC, LMAC or CMAC (cf. infra)

### Based on a block cipher: CBC-MAC (2)

Security with DES:

- Key search:  $2^{56}$  encryptions
- Key recovery using Ic:  $2^{43}$  known texts
- Guess MAC:  $\max(1/2^{56}, 1/2^m)$
- Birthday forgery attack (even if triple-DES):
  - $m = 64$ :  $2^{32}$  known and 1 chosen text
  - $m = 32$ :  $2^{33}$  chosen texts
- Improved attack for  $m = 32$ :  $2^{17}$  chosen texts and 2 known texts [Knudsen97]

Much smaller than expected!

### Based on a block cipher: CBC-MAC (3)

Security with AES-128:

- Key search:  $2^{128}$  encryptions
- Guess MAC:  $1/2^m$
- Birthday forgery attack:
  - $m = 128$ :  $2^{64}$  known and 1 chosen text
  - $m = 64$ :  $2^{66}$  chosen texts
- Improved attack for  $m = 64$ :  $2^{33}$  chosen texts and 2 known texts [Knudsen97]

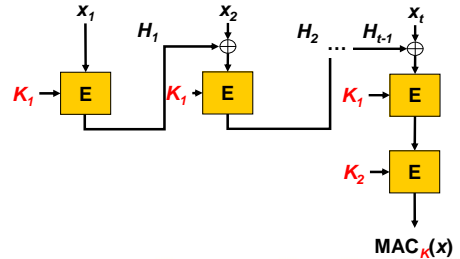
Acceptable for most applications

Exercises: CBC-MAC forgery

- simple CBC-MAC is not secure on message spaces of variable length
  - exercise: consider a 1-block input  $x$  consisting of  $n$  bits and assume that you know  $MAC_K(x)$ ; show that it is possible to find the MAC for a specific 2-block input
  - exercise: consider two 1-block inputs  $x$  and  $x'$  consisting of  $n$  bits and assume that you know  $MAC_K(x)$  and  $MAC_K(x')$ ; show that it is possible to find the MAC for a specific 2-block input

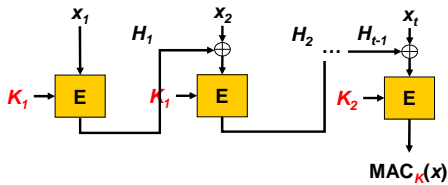
MAC based on a block cipher: EMAC

Better way to process last block: encrypted MAC (EMAC)  
[RIPE'93][Petrank-Rackoff'98]



MAC based on a block cipher: LMAC

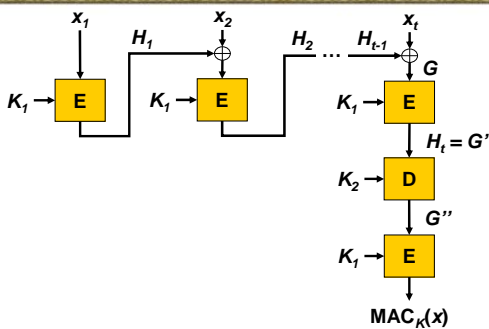
An even better way to process last block: LMAC  
[Handschuh-Preneel'06]



NIST: CMAC

- Description: use simple CBC-MAC but
  - Derive two keys from  $K_1$ :  $K_2 = E_{K_1}(0)$  and  $K'_2$  is derived from  $K_2$  with a simple finite field operation
  - XOR  $K_2$  or  $K'_2$  to the last plaintext block (first choice if no padding, second choice if there is padding)
- Evaluation
  - This saves 1 key schedule and 1 encryption (if the length of the plaintext is an exact multiple of the block length)
  - Price to pay is robustness:  $K_2$  and  $K'_2$  can be recovered with an internal collision attack
  - Banks send the value  $K_2 = E_{K_1}(0)$  as (public) key confirmation value!
- Note on name
  - This was called OMAC by its designers [Iwata-Kurosawa]
  - OMAC is an optimized version of TMAC which is an optimized version of XCBC [Black-Rogaway'00]

MAC based on a block cipher: retail MAC



Based on a block cipher: retail MAC (2)

- Security with DES and  $m = 64$ :
- Key search:  $2^{112}$  encryptions
  - Guess MAC:  $\max(1/2^{56}, 1/2^m)$
  - (first attack is based on guessing  $K_1$ )
  - Birthday forgery attack:  $2^{32}$  known and 1 chosen text
  - Improved key recovery [Preneel-van Oorschot-Knudsens]
    - $2^{32.5}$  known texts and  $3 \cdot 2^{56}$  off-line encryptions
    - 1 known text +  $2^{56}$  MAC verifications +  $2^{57}$  off-line encryptions
- Solution: triple-DES in first and last round?

### MAC based on a block cipher: Mac-DES (1)

[Knudsen-Preneel'98]

### Based on a block cipher: Mac-DES (2)

Security with DES and  $m = 64$ :

- Key search:  $2^{112}$  encryptions
- Guess MAC:  $\max(1/2^{112}, 1/2^m)$
- Birthday forgery attack:  $2^{32}$  known and 1 chosen text
- Improved key recovery [Coppersmith-Mitchell-Knudsen2000]:
  - $2^{48}$  chosen texts and  $2^{59}$  off-line encryptions

Included in ISO/IEC 9797-1 (revision, 1999)

### MAC: based on an MDC?

- **Secret prefix:**  $h(K_1||x)$   
Prepend length to avoid that one can compute  $h(K_1||x||y)$  from  $h(K_1||x)$  without knowing  $K_1$
- **Secret suffix:**  $h(x||K_2)$   
Off-line attacks on  $h$
- **Envelope:**  $h(K_1||x||K_2)$   
Risky: less secure than  $h$
- Better variants:
  - MDx-MAC and H-MAC:
  - $h_K(x) = h(h(K_1||x)||K_2)$

### HMAC

- HMAC keys through the IV (plaintext) [Kim+'06]
  - collisions for MD5 invalidate current security proof of HMAC-MD5
  - new attacks on reduced version of HMAC-MD5 and HMAC-SHA-1

	Rounds in f2	Rounds in f1	Data complexity
Haval-4	128	102 of 128	$2^{254}$ CP
MD4	48	48	$2^{72}$ CP + $2^{77}$ time
MD5	64	33 of 64	$2^{126.1}$ CP
MD5	64	64	$2^{51}$ CP & $2^{100}$ time (RK)
SHA-0	80	80	$2^{109}$ CP
SHA-1	80	53 of 80	$2^{98.5}$ CP

no problem yet for most widely used schemes

### Information-theoretic authentication

Authentication codes (AC): unconditionally secure  
= independent of computational power of opponent

- Research area since mid 1970s
- Widely believed to be impractical:
  - Use key only once
  - Sometimes very large keys
  - Security level against forgery is at most half the key size

In 1990s series of new schemes:  
Polynomial evaluation, Toeplitz, bucket hashing, MMH, UMAC, ...

### GMAC: polynomial authentication code

(NIST SP 800-38D 2007 + 3GSM)

- keys  $K_1, K_2 \in GF(2^{128})$
- input  $x: x_1, x_2, \dots, x_t$ , with  $x_i \in GF(2^{128})$

$$g(x) = K_1 + \sum_{i=1}^t x_i \cdot (K_2)^i$$

- in practice: compute  $K_1 = \text{AES}_{K_2}(n)$  (CTR mode)

- properties:
  - lightweight and/or fast in software and hardware (support from Intel/AMD)
  - not very robust w.r.t. nonce reuse, truncation, MAC verifications, due to reuse of  $K_2$  (not in 3GSM!)
  - efficient through reuse of fast arithmetic
    - (Intel/AMD) PCLMULQD: 10.68 cycles/byte [Kasper-Schwabe09]
  - weak keys [Saarinen11][Cid-Procter'13]
  - versions over  $GF(p)$  (e.g. Poly1305-AES) seem more robust

### UMAC RFC 4418 (2006)

- key  $K, k_1, k_2, \dots, k_{256} \in GF(2^{32})$  (1024 bytes)
- input  $x: x_1, x_2, \dots, x_{256}$ , with  $x_i \in GF(2^{32})$   
 $g(x) = \text{prf}_K(h(x))$   
 $h(x) = \left( \sum_{i=1}^{512} (x_{2i-1} + k_{2i-1}) \bmod 2^{32} \cdot (x_{2i} + k_{2i}) \bmod 2^{32} \right) \bmod 2^{64}$
- properties
  - software performance: 1-2 cycles/byte
  - forgery probability:  $1/2^{30}$  (provable lower bound)
  - [Handschuh-Preneel08] full key recovery with  $2^{40}$  verification queries (no nonce reuse needed!)
  - Similar attack applies to WMAC polynomial variant

### Information-theoretic authentication

- simple
- very high speeds
  - UMAC/VMAC: up to 0.5-2 cycles/byte for long messages;
  - poly1305-AES up to 4-5 cycles/byte
- parallelizable
- hardware support by Intel (GCM)
- use key only once!
- consecutive keys can be generated with an additive stream cipher
  - but then the unconditional security is lost
- speed comes at cost of large keys (e.g. UMAC): key reuse??
- if part of keys is reused: key recovery attacks
- not robust: nonce reuse can also lead to key recovery

**Conclusion: use polynomial hash functions but avoid key reuse as specified in several standards**

### Authenticated encryption

- Default modes: ECB/CBC/CFB/OFB and CTR
- Needed for network security, but only fully understood by crypto community around 2000 (too late)
- Standards have been selected recently:
  - CCM: CTR + CBC-MAC [NIST SP 800-38C]
  - GCM: CTR + GMAC [NIST SP 800-38D]
- Both are suboptimal

Issues:

- associated data
- parallelizable
- on-line
- provable security

IAPM      GCM  
 XECB      CCM  
 OCB      (EAX)

patented

### MDC ↔ MAC

Authentication without secrecy

- MAC: obvious solution
- MDC: protect authenticity of hash result

Authentication with secrecy

- MAC: needs 2 INDEPENDENT keys (MAC then encrypt, encrypt then MAC or MAC then encrypt then MAC)
- MDC: only 1 key, but important security risks: avoid this approach
- Clear choice: authenticated encryption mode
  - Many solutions: OCB, IAPM, XECB, GCM, CCM, . . .

### Performance

- Modern processor
  - HMAC, MDx-MAC: 13.1 cycles/byte for SHA-1 and 15.8 cycles/byte for RIPEMD-160
  - CBC-MAC: 43 cycles/byte for DES and 7-14 cycles/byte for AES
  - Universal hash functions: 2-4 cycles/byte
- Better performance than encryption if one is willing to pay the price in robustness

### Practical recommendations

- CBC-MAC variant of AES (LMAC or CMAC)
- HMAC-RIPEMD-160 or HMAC-SHA-1
- Universal hash function based
  - GMAC but replace  $K_2$  for every message as in 3G
  - Poly1305-AES

## Summary

- Data authentication  $\leftrightarrow$  secrecy
- Symmetric authentication  $\leftrightarrow$  digital signature
  - MAC algorithms are much faster than signatures
- MAC algorithms: much more mature than hash functions
  - Universal hash function/information theory based: fast but lack some robustness
- Authenticated encryption better understood but not yet widely deployed
- Importance of secure protocols (serial numbers, timestamping)

